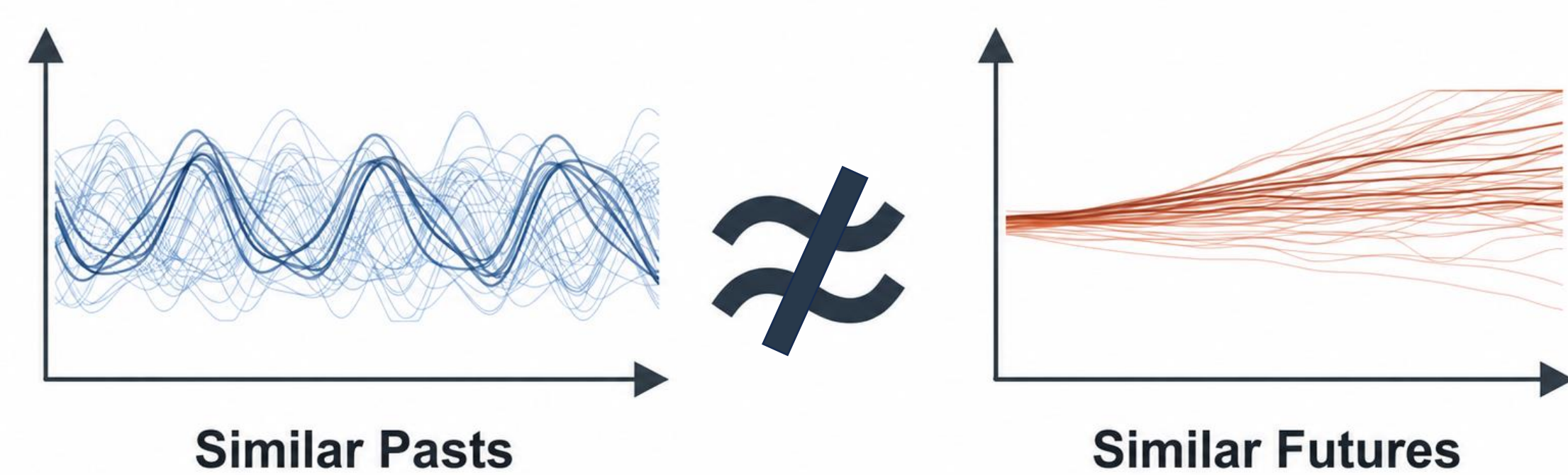


Stationarity-Aware Retrieval-Augmented Time Series Forecasting

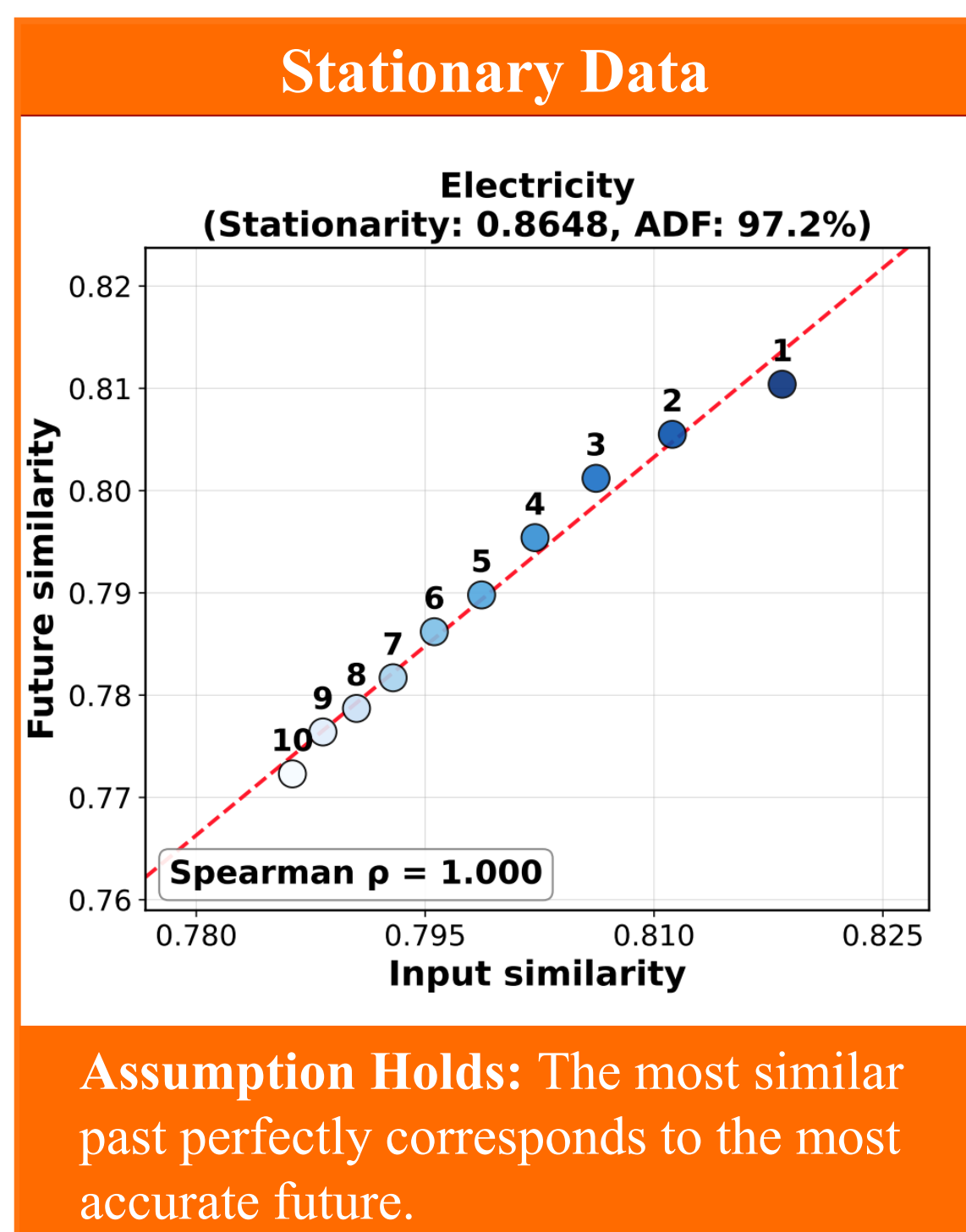
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Motivation

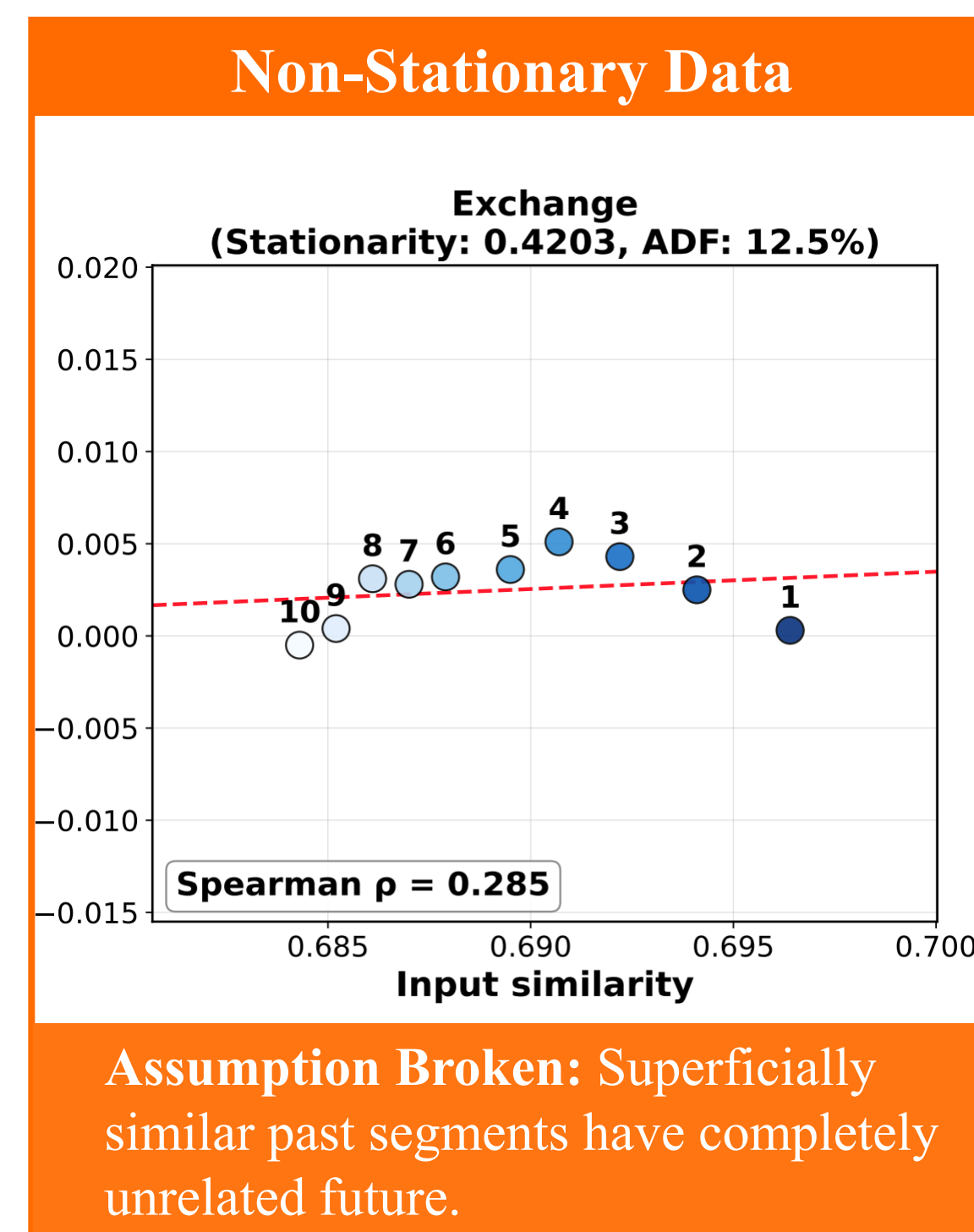
Traditional retrieval-based forecaster assumes: **similar pasts imply similar futures**. However, real-world time series are often non-stationary: **similar histories may lead to different futures**. Thus, similarity-only retrieval becomes brittle and redundant.



Examples



Assumption Holds: The most similar past perfectly corresponds to the most accurate future.



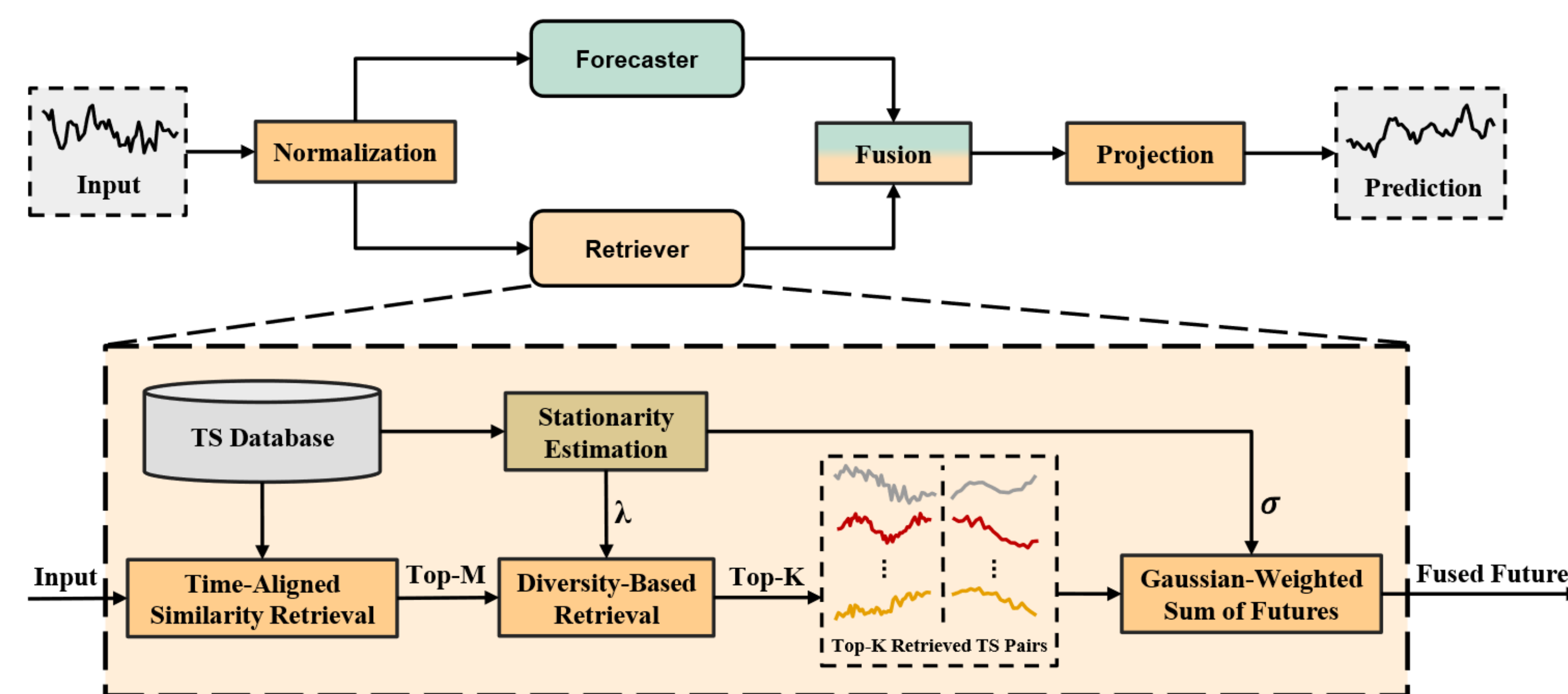
Assumption Broken: Superficially similar past segments have completely unrelated future.

Key Takeaways

- Time series similarity alone is not enough.** Under non-stationarity, similar historical patterns may lead to different futures,
- Retrieval should adapt to stationarity.** SARAF uses time-aligned matching, stationarity-guided diversity selection, and adaptive Gaussian fusion to balance relevance and diversity across different temporal regimes.
- Better retrieval improves forecasting.**

Method

Overview of SARAF:



- Stationarity Estimation.** To estimate dataset-level stationarity, We partition each sample $\mathbf{x}_i \in \mathbb{R}^{L \times C}$ into W sub-windows and compute the variation of local means and standard deviations across them. Let v_μ and v_σ denote these variations. The stationarity score $\bar{s}$ is defined by normalizing v_μ and v_σ with the global scale $\bar{\sigma}$ to achieve scale invariance.

$$\bar{s} = \frac{1}{N} \sum_{i=1}^N \tilde{s}_i, \quad \tilde{s}_i = \frac{1}{2} \left(\left[1 - \min \left(1, \frac{v_\mu}{\bar{\sigma}} \right) \right] + \left[1 - \min \left(1, \frac{v_\sigma}{\bar{\sigma}} \right) \right] \right) \in [0, 1].$$

- Time-Aligned Retrieval.** Pattern similarity alone may retrieve temporally misaligned cycles. We combine time series similarity with calendar-aware temporal cues to encourage retrieval from corresponding daily, weekly, and seasonal periods.
- Stationarity-Guided Diversity Retrieval.** Highly similar neighbors are often redundant, especially for non-stationary series. We apply MMR-based selection to the Top- M candidates from time-aligned retrieval, with the relevance--diversity trade-off controlled by stationarity:

$$\lambda(\bar{s}) = \lambda_{\min} + \bar{s}(\lambda_{\max} - \lambda_{\min}).$$

- Stationarity-Guided Gaussian Fusion.** The Top- K retrieved futures are aggregated using Gaussian-kernel weights:

$$w_k = \frac{\exp(-d_k^2 / 2\sigma(\bar{s})^2)}{\sum_{j=1}^K \exp(-d_j^2 / 2\sigma(\bar{s})^2)}, \quad \sigma(\bar{s}) = \sigma_{\min} + (1 - \bar{s})(\sigma_{\max} - \sigma_{\min}).$$

Experiment Results

Main Results

Model	SARAF (ours)		RAFT		DUET	
Metric	MSE	MAE	MSE	MAE	MSE	MAE
ETTh1	0.415	<u>0.435</u>	<u>0.418</u>	0.434	0.430	0.447
ETTh2	0.340	0.392	0.358	0.408	<u>0.358</u>	<u>0.405</u>
ETTm1	0.346	<u>0.378</u>	0.347	<u>0.377</u>	0.349	0.382
ETTm2	0.248	0.314	0.257	0.321	<u>0.254</u>	0.314
Exchange	0.394	0.415	0.449	0.444	0.469	0.446
Solar	0.206	0.258	0.211	0.255	0.198	0.245
ECL	0.152	0.251	<u>0.156</u>	0.253	0.163	0.254
Traffic	<u>0.395</u>	<u>0.280</u>	0.401	0.281	0.380	0.249

*Average performance over four horizons

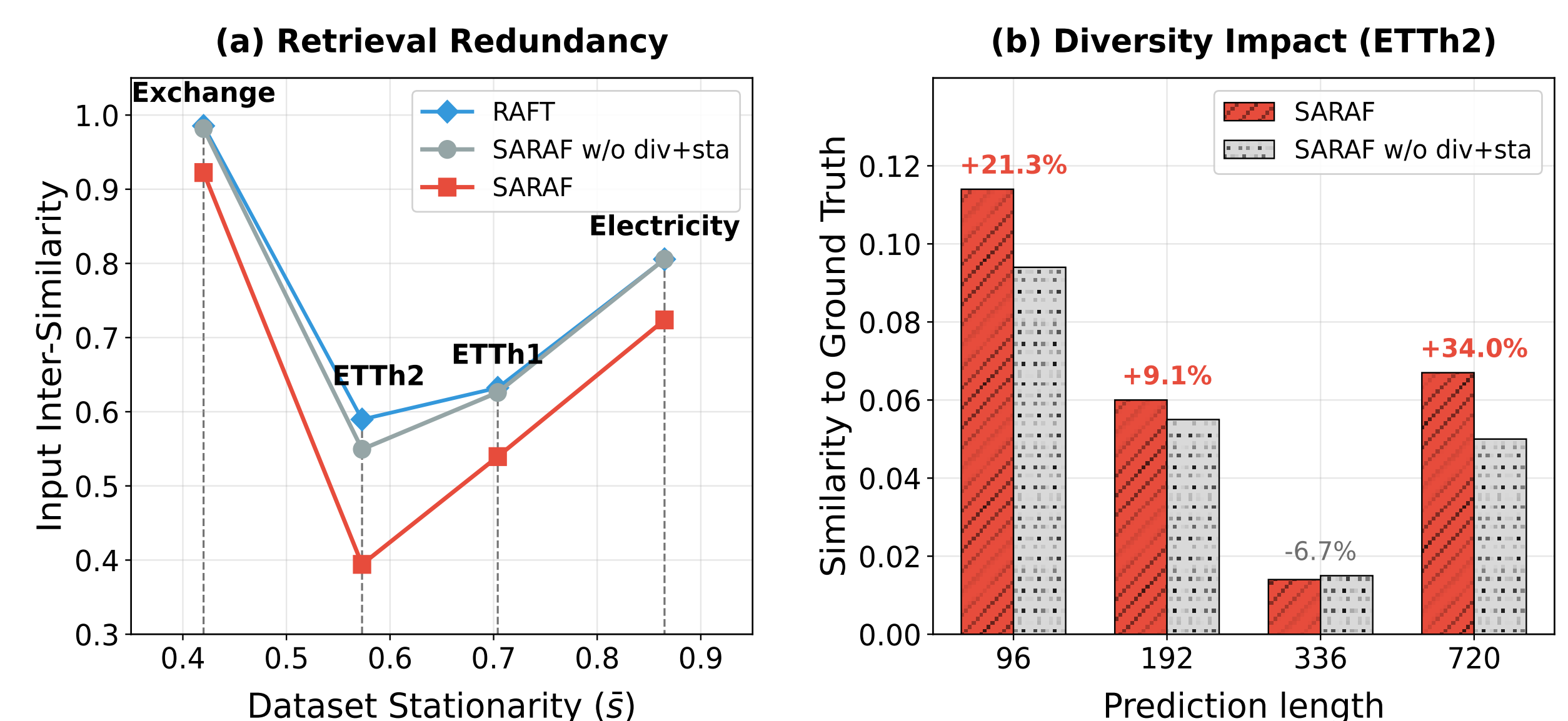
Ablation Results

Dataset	SARAF	w/o Ret	w/o For	w/o time	w/o div	w/o sta	w/o div+sta
ETTh1	0.415	0.421	1.328	0.42	0.415	0.416	0.416
ETTm1	0.346	0.359	1.272	0.347	0.347	0.348	0.348
Exchange	<u>0.394</u>	0.411	0.377	0.398	0.400	0.398	0.399
ECL	0.152	0.163	1.613	0.156	0.151	0.152	0.151
Traffic	0.395	0.414	2.768	0.402	0.396	0.396	0.397

*Average MSE over four horizons

Additional Analysis

Diversity-Based Retrieval Analysis.



Efficiency

Model	Param. (M)	Model Mem. (MiB)	All Mem. (MiB)	Speed (ms/iter)
SARAF (ours)	0.088	0.335	54.077	0.334
DUET	6.66	25.408	36.03	7.202
RAFT	0.104	0.397	122.996	0.59