



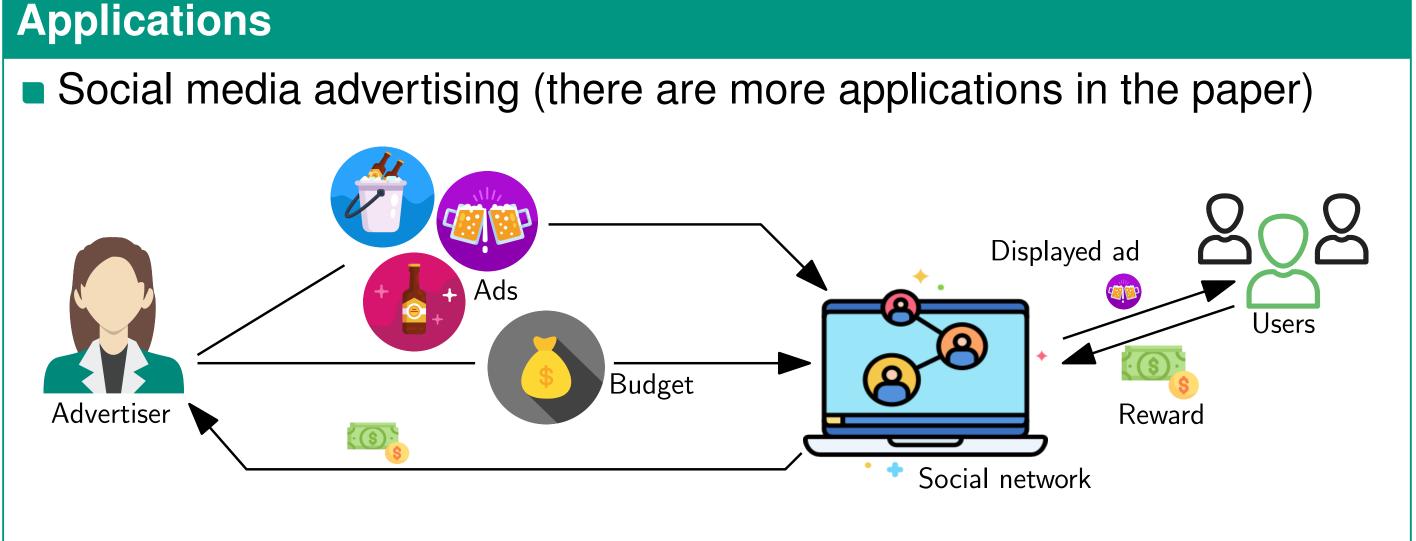


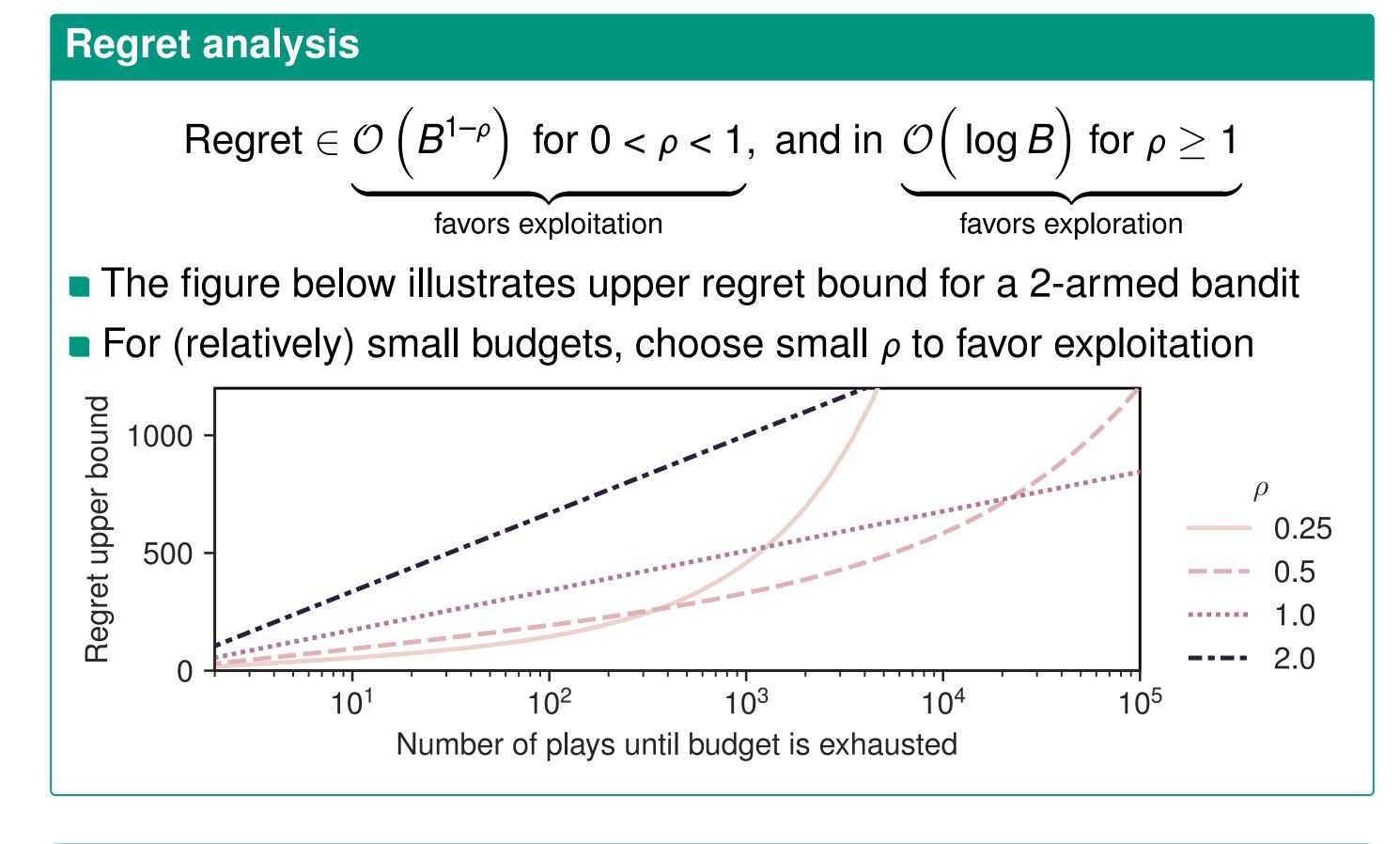
Budgeted Multi-Armed Bandits with Asymmetric Confidence Intervals

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Budgeted Multi-Armed Bandits ■ While budget *B* not empty: Play one of K arms Observe reward, pays cost (both are random) Update strategy arm 1 reward update choose arm statistics arm 2 of arm $\operatorname{arm} K$ - Budget > 0? -

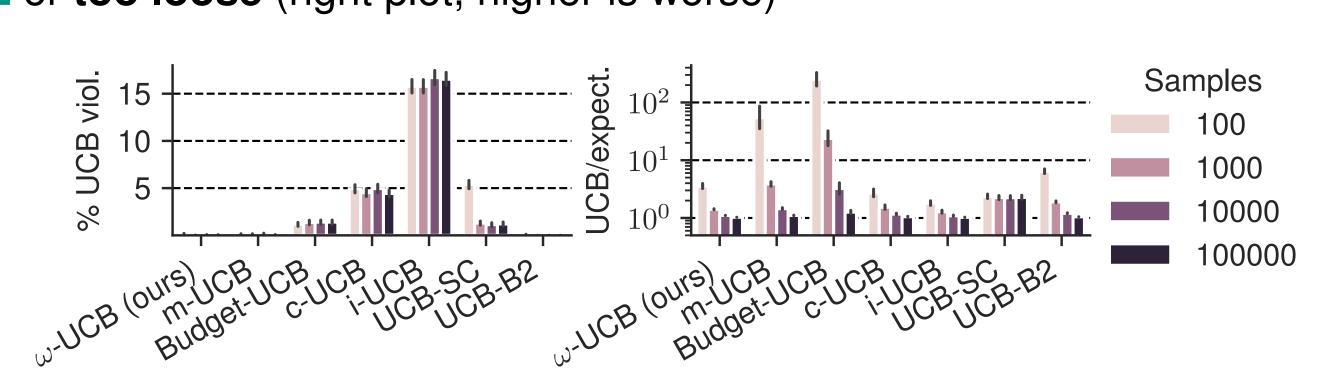
Our Algorithm – ω -UCB Upper confidence bound (UCB) sampling ■ Choose arm with highest UCB of reward-cost ratio "optimism under uncertainty" Compute UCB using asymmetric confidence interval ■ Increase confidence level over time according to $\sqrt{1-t^{-\rho}}$ ρ : scaling parameter of confidence interval observe play arm with highest UCB play all reward and pay arms once cost update update UCB statistics of all arms played arm





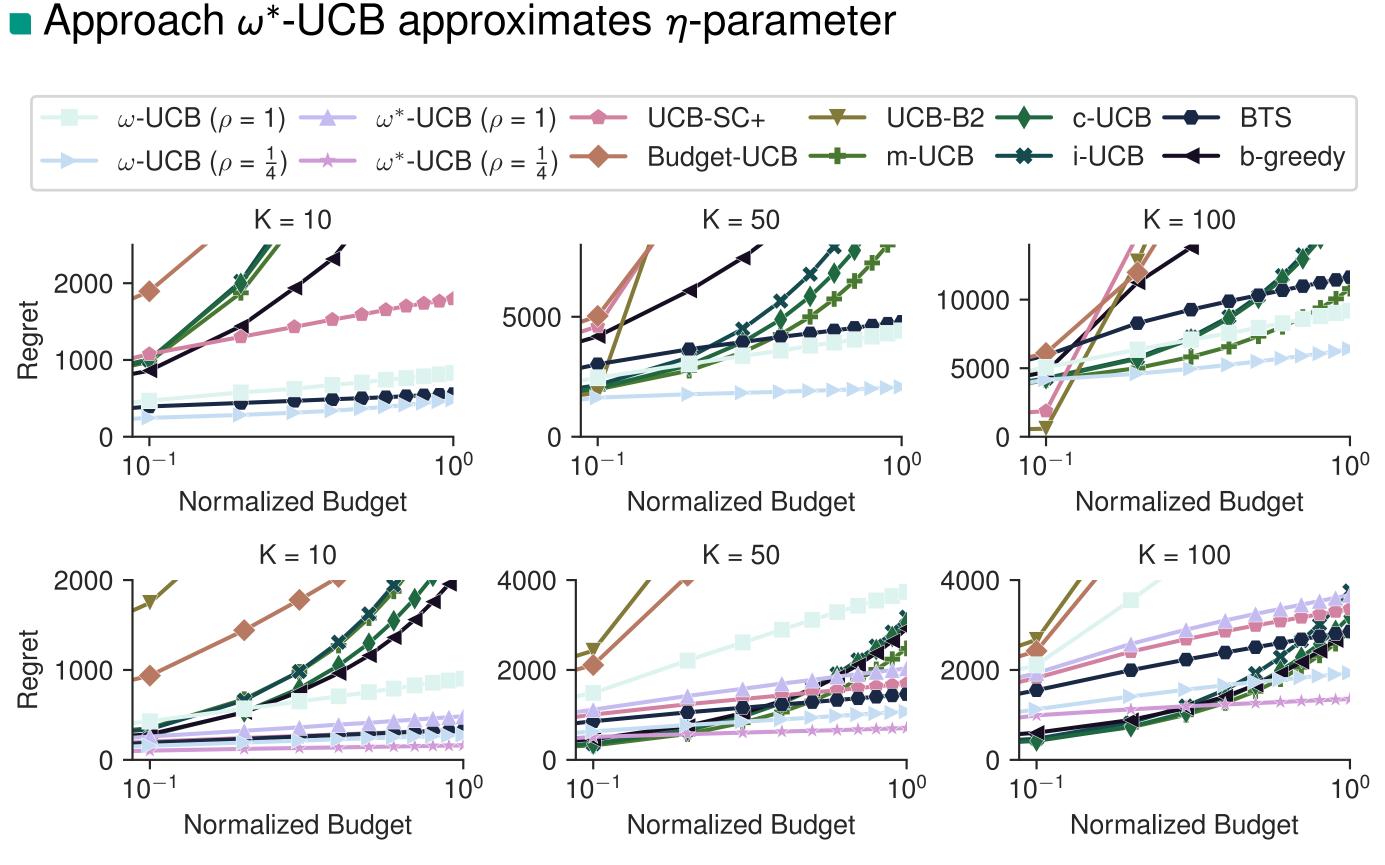
Related work

- Upper confidence bound (UCB) sampling: m-UCB, i-UCB, c-UCB [1], Budget-UCB [2], UCB-SC [3], UCB-B2 [4]
- UCB is often either too tight (left plot, higher is worse)
- or **too loose** (right plot, higher is worse)



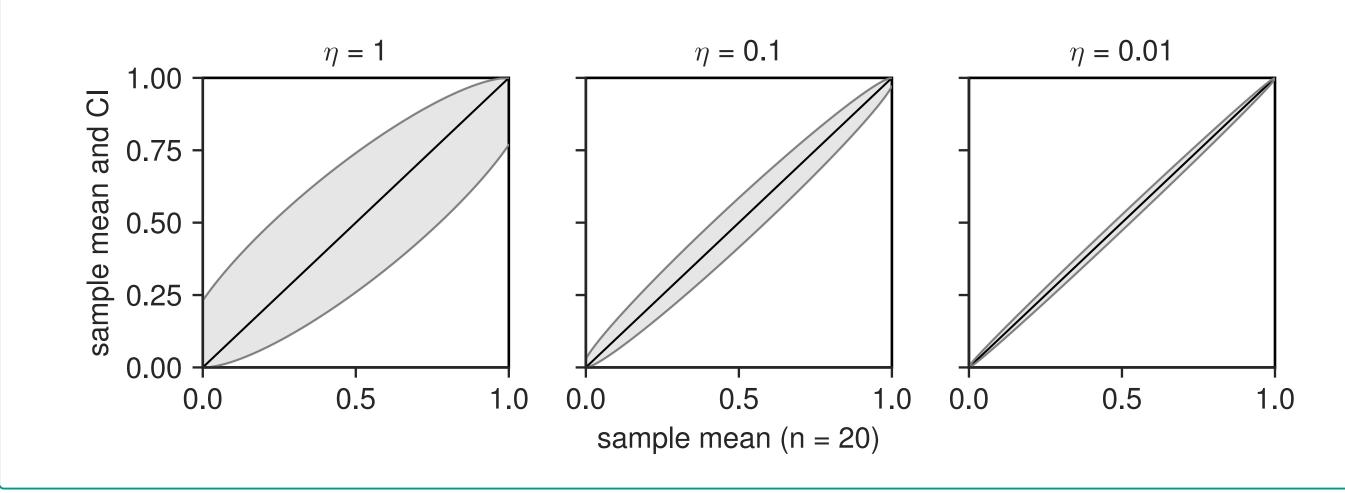
Experiments on synthetic data

- First row: Bernoulli distributed rewards and costs
- Second row: rewards and costs sampled from {0, 0.25, 0.5, 0.75, 1}



Asymmetric confidence intervals

- Generalization of the Wilson Score Interval for binomial proportions [5]
 - (refer to the paper for the math)
- Figure illustrates asymmetry of confidence interval
- $\eta \in [0, 1]$: variance relative to Bernoulli variable with same mean
- Confidence interval stays within bounds of random variable



- [1] Y. Xia, T. Qin, W. Ding, et al., "Finite budget analysis of multi-armed bandit problems," Neurocomputing, vol. 258, pp. 13–29, 2017, ISSN: 0925-2312.
- [2] Y. Xia, W. Ding, X.-D. Zhang, N. Yu, and T. Qin, "Budgeted Bandit Problems with Continuous Random Costs," in ACML, ser. JMLR Workshop and Conference Proceedings, vol. 45, JMLR.org, 2015, pp. 317–332.
- [3] R. Watanabe, J. Komiyama, A. Nakamura, and M. Kudo, "KL-UCB-Based Policy for Budgeted Multi-Armed Bandits with Stochastic Action Costs," IEICE Trans. Fundam. Electron. Commun. Comput. Sci., vol. 100-A, no. 11, pp. 2470–2486, 2017.
- [4] S. Cayci, A. Eryilmaz, and R. Srikant, "Budget-constrained bandits over general cost and reward distributions," in AISTATS, S. Chiappa and R. Calandra, Eds., ser. PMLR, vol. 108, PMLR, 2020, pp. 4388–4398.
- [5] E. B. Wilson, "Probable Inference, the Law of Succession, and Statistical Inference," Journal of the American Statistical Association, vol. 22, no. 158, pp. 209–212, 1927.