

# Efficient Subspace Search in Data Streams

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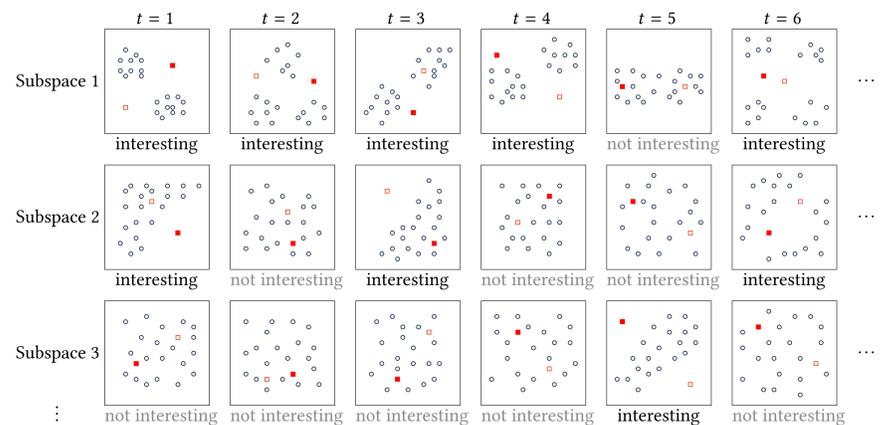
Information Systems, Elsevier (In press). Preprint: [arXiv:2011.06959](https://arxiv.org/abs/2011.06959)

## Motivation

- **Data streams are everywhere**
  - Network traffic, sensor data, financial transactions, ...
- **Mining patterns (outliers, clusters) must take place in real time**
  - Difficulties: curse of dimensionality & concept drift
- **“Ensemble” Feature Selection: Subspace Search**
  - Goal: find relevant projections, as in [2]
  - So far only works for specific algorithms, or static data
- **Subspace Search requires:**
  - A quality measure (how “good” is a given projection)
  - A search scheme (explore the exponential set of subspaces)
  - → We extend this idea to the streaming setting
- **Stream constraints:** Efficiency, Single Scan, Adaptation, Anytime

- “Searching for outliers in high-dimensional data is like searching for a needle in a haystack, while the haystack “hides” among an exponential number of haystacks” [3].

- **Data streams:** The haystacks and needle location can also change.



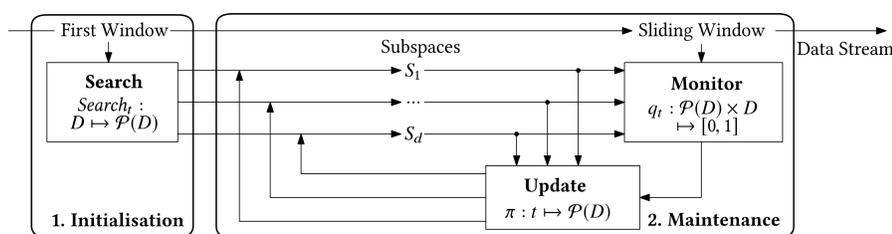
## Related Work

- Subspace search for static data: [2, 5, 6]
- Subspace search for data streams: [7, 8]
  - Only for specific static Data Mining algorithms
- Closest competitor: StreamHiCS [9]
  - Boils down to a periodic repetition of the procedure in [2]
- The most similar approach to ours, but for static data: GMD [6]
- Outlier detectors: xStream [10], RS-Stream [11]

## Our Contributions

- **SGMRD: Streaming Greedy Maximum Random Deviation**
  - A new method for “general” subspace search in data streams
  - SGMRD leverages novel multivariate dependency measures and Multi-Armed Bandit (MAB) algorithms
  - Monitoring subspaces in data streams improves the performance of subsequent mining tasks, e.g., outlier detection
- **Code, data:** <https://github.com/edouardfouche/SGMRD>

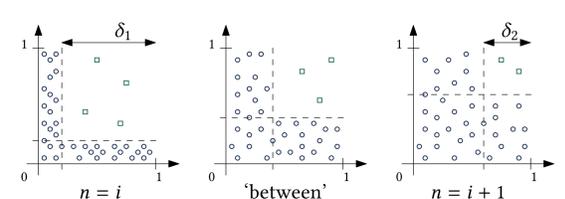
## Our Approach & Experiments



Characteristics of the benchmark data sets

Benchmark	# Instances	# Dimensions	% Outliers
PYRO	10,000	100	NA
KDDCUP99	25,000	38	7.12
ACTIVITY	22,253	51	1
BACKBLAZE	12,600	44	10
CREDIT	284,807	29	0.17
SYNTH10	10,000	10	0.86
SYNTH20	10,000	20	0.88
SYNTH50	10,000	50	0.81

Our synthetic benchmark generation



### Search: Greedy dimension-based scheme

- Returns one single subspace per dimension  $d$ , as in [6]
- This subspace maximizes quality w.r.t.  $d$

### Monitor: Quality as a “contrast” measure

- **Contrast:**  $q_t(S, s_i) = 1 - \frac{1}{M} \sum_{m=1}^M T(\hat{p}(S|s_i), \hat{p}(S|\bar{s}_i)) \in [0, 1]$
- **Smoothing:**  $Q_{t+1}(s_i) = \gamma * q_t(S, s_i) + (1 - \gamma) * q_{t+1}(S, s_i)$

### Update: Policy based on (Multiple-Play) Multi-Armed Bandit

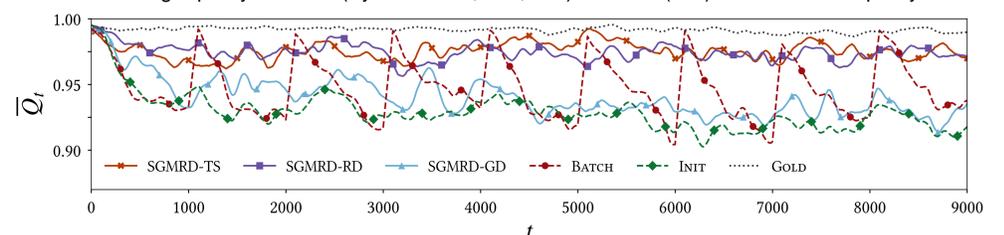
- **Success:** The search w.r.t.  $s_i$  yields a better subspace (1)
- **Failure:** The search w.r.t.  $s_i$  did not yield a better subspace (0)
- We use a strategy based on Thompson Sampling (TS) [12]

### Downstream Data Mining

- Virtually any task: outlier detection, clustering, predictions...
- We focus on outlier detection (with Local Outlier Factor (LOF))

→ For more details and experiments, see [1]

Average quality at time  $t$  (Pyro data set,  $L=1, v=2$ ): SGMRD(-TS) maximizes the quality



Outlier detection: SGMRD outperforms its competitors in terms of ROC AUC, precision, recall

Approach	AUC	AP	P1%	P2%	P5%	R1%	R2%	R5%
SGMRD	97.32	85.39	94.59	94.83	94.24	9.44	18.97	47.10
LOF	93.93	61.80	74.32	64.72	64.03	7.42	12.94	32.00
STREAMHiCS	88.52	47.38	70.72	54.61	51.89	7.06	10.92	25.93
RS-STREAM	95.95	68.23	71.62	72.58	75.00	7.15	14.52	37.48
xSTREAM	77.71	20.41	3.60	10.14	16.31	0.36	2.02	8.13
SGMRD	69.98	10.29	0.00	0.20	0.56	0.00	0.06	0.39
LOF	56.92	1.65	2.38	3.57	2.38	2.38	7.14	11.90
STREAMHiCS	79.22	46.07	50.79	26.59	10.95	50.79	53.17	54.76
RS-STREAM	80.55	7.17	7.14	13.49	9.37	7.14	26.98	46.83
xSTREAM	76.86	3.69	1.59	3.17	6.19	1.59	6.35	30.95
SGMRD	90.91	13.31	7.14	18.65	15.40	7.14	37.30	76.98
LOF	56.92	1.65	2.38	3.57	2.38	2.38	7.14	11.90
STREAMHiCS	79.22	46.07	50.79	26.59	10.95	50.79	53.17	54.76
RS-STREAM	80.55	7.17	7.14	13.49	9.37	7.14	26.98	46.83
xSTREAM	76.86	3.69	1.59	3.17	6.19	1.59	6.35	30.95
SGMRD	75.87	31.27	27.00	16.00	7.60	33.33	39.51	46.91
LOF	61.38	1.08	0.00	0.50	0.60	0.00	1.23	3.70
STREAMHiCS	63.90	12.00	11.00	6.00	3.40	13.58	11.81	20.99
RS-STREAM	46.52	0.73	0.00	0.00	0.00	0.00	0.00	0.00
xSTREAM	48.43	0.90	1.00	0.50	1.40	1.23	1.23	8.64
SGMRD	95.06	15.87	10.69	7.47	3.22	55.51	77.57	83.65
LOF	91.50	4.67	6.22	5.20	2.69	32.32	53.99	69.96
STREAMHiCS	89.21	3.48	3.59	2.93	2.28	18.63	30.42	59.32
RS-STREAM	85.13	1.63	2.27	2.49	1.86	11.79	25.86	48.29
xSTREAM	94.62	9.10	10.83	6.48	3.18	56.27	67.30	82.51

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